The 2nd Asian Nuclear Reaction Database Development Workshop

> CNDC of CIAE and AASPP of JSPS

Beijing, China September 06,, 2011



This document was prepared as an account of work to present in the 2nd Asian Nuclear Reaction Database Development Workshop



A comparison of ternary fragmentation potential energy surface in equatorial and collinear configuration

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Thanks



THANKS FOR THIS OPPORTUNITY





In 2008, I got an opportunity to interact with Prof. S. Ganesan in a meeting at Tirunelveli and initiated a project proposal which was later sanctioned and supported by DAE-BRNS, Govt. of India in 2009. (On going)

In 2008 we at BU, attended couple of nuclear data related meetings at Manipal University, Manipal during 25th to 28th February, 2008 and the other one during October 2-4, 2008.

The first meeting was on Covariance error matrices (Prof. Leeb) and in the later meeting Dr. R. Capote conducted a demonstrative program for the use of EMPIRE code.



In 2009, we actively participated in the third DAE-BRNS Theme Meeting on EXFOR Compilation of Nuclear Data, November 03-07, 2009, Jaipur, Rajastan, India.

Dr. D. Svetlena, IAEA demonstrated about how to make entries in the EXFOR and also about the digitizer software. (Inpgraph)

All the participants with the support of Dr. D. Svetlena and other experts made several entries during that meeting.

Following entries were made by us





ENTRY	D6022
TITLE	Measurement of near and above barrier fusion excitations for 7-Li+28-Si
AUTHOR	H.Majumdar, Mandira, Sinha, P.Basu, R.Bhattacharya, Subinit Roy, S.Santra, M.Biswas, V.V.Parkar, B.R.Behra, K.S.Golda, S.K.Datta, S.Kailas
Compiled by	K. Manimaran, Megha Bhike, C. Karthik
ENTRY	<u>D6062</u>
TITLE	Proton and alpha evaporation spectra in low energy C-12 and O-16 induced reactions
AUTHOR	E.T.Mirgule, D.R.Chakrabarty, V.M.Datar, Suresh Kumar, Mitra, H.H.Oza
Compiled by	Megha Bhike, K. Manimaran, C. Kartik
ENTRY	<u>D6089</u>
TITLE	13-C(alpha,neutron)16-O recation cross section between 1.95 and 5.57 MeV
AUTHOR	K.K.Sekheran, A.S.Divatia, M.K.Metha, S.S.Kerekatte, K.B.Nambiar
Compiled by	K. Manimaran, Megha Bhike, C. Karthik
ENTRY	<u>D6021</u>
TITLE	Direct and compound reactions induced by unstable helium beams near the Coulomb barrier
AUTHOR	A.Navin, V.Tripathi, Y.Blumenfeld, V.Nanal, C.Simenel, M.Casandjian, G.de France, R.Raabe, D.Bazin, A.Chatterjee, M.Dasgupta, S.Kailas, R.C.Lemmon, K.Mahata, R.G.Pillay, E.C.Pollacco, K.Ramachandran, M.Rejmund, A.Shrivastava, J.L.Sida, E.Tryggestad
Compiled by	G.Pandikumar, Dr. S. Ganesan, Dr.M.Balasubramaniam, Joseph Jermiah





ENTRY	<u>D6039</u>										
TITLE	Complete and Incomplete Fusion Reactions of O-16 with As-75 at Incident Energies below 7MeV/A										
AUTHOR	R.Gun, D S.K.Saha										
Compiled by	G.Pandikumar, Dr.S.Ganesan, Dr.M.Balasubramaniam, J.Joseph Jeremiah, P.Balaji										
ENTRY	<u>D6051</u>										
TITLE	Sub-barrier fusion excitation for the system 7Li+28Si										
AUTHOR	Mandira Sinha, H.Majumdar, P.Basu, Subinit Roy, R.Bhattacharya, M.Biswas, M.K.Pradhan, S.Kailas										
Compiled by	G.Pandikumar, Dr.S.Ganesan, Dr.M.Balasubramaniam, J.JosephJeremiah										
ENTRY	<u>D6085</u>										
TITLE	REACTION 55-MN(P,N)55-FE FROM EP=1.35 TO 5.42 MEV										
AUTHOR	Y.P.Viyogi, P.Satyamurthy, N.K.Ganguly, S.Kailas, S.Saini, M.K.Mehta										
Compiled by	G.Pandikumar, Dr.S.Ganesan, Dr. S.Kailas, J.Joseph Jeremiah, Dr.M.Balasubramaniam										





In April 2011, Chanidgarh Exfor meeting

Thanks to **GSYS**

We made couple of entries, In particular D6121 was coded by us with 41 subentries

We helped others To the Exfor, Inpgraph And Gsys.

D6121 - Not	tepad				x
File Edit For	rmat View Help				
ENTRY	D6121 20110404	D6121	0	1	
SUBENT	D6121001 20110404 11 19	D6121	1	2	Ξ
TITLE	Fission time scale from prescission neutron, proton,	D6121	ī	3	
	and a particle multiplicities in 28Si+175Lu	D6121	1	4	
AUTHOR	(K.Ramachandran, A.Chatterjee, A.Navin, K.Mahata,	D6121	1	5	
	A.SIIFIVASLAVA, V.IFIPALIII,S.KAIIAS,V.NAIIAI,K.G.PIIIAY, A Sayena P.G. Thomas Suresh Kumar P.K.Sahu)	D6121	1	7	
INSTITUTE	(3INDTRM, 3INDTAT)	D6121	î	8	
REFERENCE	(J,PR/C,73,064609,2006)	D6121	1	9	
	#doi:10.1103/PhysRevC.73.064609	D6121	1	10	
	(VDG,SINDIAL) Target 1 5 mg/cm2 self-supporting foil of 175 Lu	D6121	1	12	
DETECTOR	(SISD)centered at 140 degree	D6121	ī	13	
METHOD	(EDE)neutron,proton alpha emission measurement	D6121	1	14	
INC-SOURCE	(POLIS)pulsed 159-MeV 28Si beam from LINAC booster	D6121	1	15	
HISTORY	(20110404C) M.Balasubramanlam,Vijayaragnavan, Karthikrai Bharathiar Univ Rajeshkumar NTT Hamirpur	D6121	1	17	
	S.Mahadevan Amrita Univ., S.Subramanian VOC College TN	.D6121	i	18	
	G.Pandikumar, IGCAR	D6121	1	19	
COMMENT	Figure 2 measurement at different angles at same	D6121	1	20	
ENDRTR	energies 10 0	D6121	1	21	
NOCOMMON		D6121	i	23	
ENDSUBENT	22 0	D6121	199	999	
SUBENT	D6121002 20110404	D6121	2	1	
BIR	2 (71-111-175(14-ST-28 X)0-NN-1 PR MLT NU/DA/DE)	D6121	2	2	
STATUS	(APRVD)	D6121	2	4	
ENDBIB	2 0	D6121	2	5	
COMMON	2 3	D6121	2	6	
		D6121	2	8	
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ENDCOMMON	3 0	D6121	2	10	
DATA	2 10	D6121	2	11	-
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- 1. Introduction
- 2. The three cluster model
- 3. α -accompanied fission of ²⁵²Cf
- 4. Role of deformation and orientation
- 5. PES of ²⁵²Cf in equatorial and collinear configuration
- 6. Summary

1. Introduction



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Superheavy elements are the trans-actinide elements beginning with Rutherfordium (Z=104). They have all been made artificially and currently have no practical purpose because of their very short life times from few minutes to few milliseconds making the studies very hard and serve purpose only for research.

The fundamental interest in heavy element research is connected to the questions

How many elements may exist in nature ? How heavy can nuclei be ? How do nuclei behave in the presence of strong Coulomb forces? What would be the next magic numbers for proton and neutron?

These kind of studies helps as a stringent test to know the validity of existing theoretical models.





- No consensus: (For Island of stability)
- In mid-1960s, a number of theoretical calculations predicted that an atom with the doubly-magic nucleus containing 114 protons and 184 neutrjons should be extra stable.
- Different parametrization within the Skyrme HF and RMF produce quite different predictions for the next spherical doubly magic nuclei
- namely Z =114, 120 and/or 126 with N =172 or 184. (Spherical RMF, Axially deformed RMF, SHF with different parameter sets which reproduces the g.s. properties)
- effective field theory predicts Z =120 and N =172 and Z =120 and N =258 as possible spherical doubly magic superheavy nuclei.

Experimental challenge



- Over the last thirty years, experimentalists are undergoing an expedition to explore the predicted "island of superheavy elements"—a region of increasingly stable nuclei around atomic number 114
- So far they have reported, on average, the discovery of one new element every two and a half years.



Latest discovery





- a new element with atomic number 117. Two isotopes of the new, still unnamed, element were produced from nuclear fusion reactions from a beam of ⁴⁸Ca ions that impinged on target nuclei of ²⁴⁹Bk. (Published in PRL 104(2010)142502). (JINR, RIAR, LLNL, ORNL, VU and UON) – Lead by Yu.Ts. Oganessian
- This was a 2 year campaign began at the High Flux Isotope Reactor in Oak Ridge with a 250-day irradiation to produce 22 mg of berkelium. (3.5 Million dollars, J. Hamilton, A.V. Ramayya of VU)
- followed by 90 days of processing at ORNL to separate and purify the berkelium, target preparation at Dimitrovgrad,
- 150 days of bombardment at most powerful HI accelerators at Dubna
- Data analysis at Livermore and Dubna, and assessment and review of the results by the team.
- This discovery fills the gap between elements 116 and 118, so that now elements are continuously known from Z=1 up to element 118



Gamma emission

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Beta decay







S. L. Muga et.al. (1961)









- Ternary fission is defined as a nuclear break-up into three fragments which covers a spectrum of fission events from one end in which a scission neutron accompanies two main fission fragments, to the other in which three fragments of about equal masses are emitted.
- The ternary fission process with three charged particles in the outgoing channel, with the third particle being very light compared to the fission fragments are called as particle accompanied fission or light charged particle accompanied fission.
- The spontaneous break-up into three nuclei of about equal mass the so called true ternary fission has not yet been observed but theoretically is being studied.



Finite Street

First evidence of TF was reported by Alvarez in 1943, ²³⁵U(n,TF) with the emission of alpha particles along with main fission fragments.

(Based on LDM in 1958, Swiatecki predicted TF, Quaternary and Quinary Fission)

In TF, the light charged particles are born along with main fragments at scission configuration.

The Coulomb force will then expel the light particle roughly at right angles to the heavy fragments motion (also supported by the measured energy spectra and angular distribution.) (U -> Ba + Kr + Alpha)



This process is a rare one as it occurs about once in ~260 binary fission events, in 252 Cf.

In TF in some cases the light cluster is also born in an excited state, and decays to ground state by emitting gamma rays.

Though a rare process, a major interest has been mounted to obtain additional data to know more about the dynamics.

Experiments on TF gives, evidence for two different modes of ternary fission, hot and the cold.

In alpha accompanied fission of ²⁵²Cf the majority of the fissions are hot, while for ¹⁰Be-accompanied fission the cold process dominates – as supported by theory



Cold ternary decays should produce all the three fragments at very low excitation energy and, consequently, with very high kinetic energies – very compact shapes at the scission point and deformations close to those of their g.s.



(F. Gonnenwein et al)



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LCP	Reaction	Energy	MPE	Angle
		(MeV)	(MeV)	
^{1}H	$^{252}Cf(sf)$	3.3-12	3.5 ± 0.5	91°
^{1}H	$^{252}Cf(sf)$	3.18-19.62	9±2	-
^{2}H	$^{252}Cf(sf)$	3.83-18.22	7±2	-
^{2}H	$^{252}Cf(sf)$	4.2-18	-	91°
^{3}H	$^{252}Cf(sf)$	3.89-23.13	8±1	-
^{3}H	$^{252}Cf(sf)$	5-24	-	91°
^{3}He	$^{252}Cf(sf)$	10.75-33.75	17 ± 1	-
^{4}He	$^{252}Cf(sf)$	7.75-34.75	16 ± 0.5	-
^{4}He	$^{252}Cf(sf)$	9-26	16.0 ± 0.3	-
^{4}He	$^{252}Cf(sf)$	7.1-41	-	92°
^{4}He	$^{252}Cf(sf)$	-	-	82°
^{4}He	$^{262}Cf(sf)$	11-40	15.6 ± 0.2	-
^{4}He	$^{252}Cf(sf)$	8-30	15.7 ± 0.2	90°
^{4}He	$^{252}Cf(sf)$	9-30	-	-
^{4}He	$^{252}Cf(sf)$	0-30	18.0 ± 0.5	-
^{4}He	$^{252}Cf(sf)$	12-32	15.6 ± 0.2	-
^{4}He	$^{250}Cf(sf)$	14-30	16.1 ± 0.1	-
^{4}He	$^{256}Fm(sf)$	14.5-31	15.5 ± 0.4	-
^{4}He	$^{257}Fm(sf)$	15-35	15.9 ± 0.6	-
^{4}He	$^{244}Pu(sf)$	12-40	15.5 ± 0.55	-
⁵ He	$^{252}Cf(sf)$	-	12.3 ± 0.9	30-150°
⁵ He	$^{252}Cf(sf)$	-	12.4 ± 0.3	-
⁵ He	$^{252}Cf(sf)$	11-12	11 ± 0.5	-
⁵ He	$^{252}Cf(sf)$	10.75-33.25	13 ± 1	-
⁶ He	$^{252}Cf(sf)$	14.6-43	-	93°
⁶ He	$^{252}Cf(sf)$	10-22	12.3 ± 0.5	90°
⁸ He	$^{252}Cf(sf)$	12-36	≤ 13	-
^{8}He	$^{252}Cf(sf)$	9.6-46	-	-
Li	$^{252}Cf(sf)$	19-39	-	-
Li	$^{252}Cf(sf)$	15.7-65	-	-
Li	$^{252}Cf(sf)$	17-35	14.3 ± 10	84.9°
Be	$^{252}Cf(sf)$	33-41	-	-
^{10}Be	$^{252}Cf(sf)$	24-73	-	-
^{10}Be	$^{252}Cf(sf)$	18.8 ± 0.4	-	-
B	$^{252}Cf(sf)$	-	20.5 ± 1	-
B	$^{252}Cf(sf)$	25-50	26 ± 0.5	-
C	$^{252}Cf(sf)$	32-34	-	-
^{14}C	$^{262}Cf(sf)$	30-50	34 ± 0.5	-

$\begin{array}{c c c c c c c c c c c c c c c c c c c $	LCP	Reaction	Energy	MPE	Yield
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			(MeV)	(MeV)	
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	^{3}H	$^{235}U(n, f)$	-	8.0 ± 0.2	-
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{3}H	$^{235}U(n, f)$	5-18	15.8 ± 0.1	-
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{3}H	$^{233}U(n, f)$	5-18	15.8 ± 0.1	-
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	³ H	$^{239}Pu(n, f)$	5-18	15.9 ± 0.2	-
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	³ H	$^{241}Pu(n, f)$	5-18	15.9 ± 0.3	-
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{4}He	$^{233}U(n, f)$	10-34	15.8 ± 0.1	-
	^{4}He	$^{235}U(n, f)$	8-26	15.4 ± 0.2	-
	^{4}He	$^{235}U(n, f)$	10-32	15.8 ± 0.1	-
	^{4}He	$^{239}Pu(n, f)$	8-34	15.9 ± 0.1	-
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{4}He	$^{241}Pu(n, f)$	10-35	15.9 ± 0.1	-
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{4}He	$^{232}Th(n, f)$	8-28	15.8 ± 0.2	-
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	⁵ He	$^{235}U(n, f)$	11	11.6 ± 1.4	-
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	⁸ Li	$^{249}Cf(n, f)$	-	15.1 ± 1.4	$2.6\pm0.7\times10^{-6}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	⁹ Li	$^{249}Cf(n, f)$	-	12.5 ± 0.9	$3.8\pm1.6\times10^{-6}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{10}Be	$^{249}Cf(n, f)$	-	17.5 ± 0.4	$3.8\pm0.7\times10^{-5}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{11}Be	$^{249}Cf(n, f)$	-	16.5 ± 1.3	$4.7\pm1.2\times10^{-6}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{12}Be	$^{249}Cf(n, f)$	-	15.1 ± 1.1	$2.7\pm0.7\times10^{-6}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{12}Be	$^{249}Cf(n, f)$	-	21.8 ± 0.3	$1.5\pm0.4\times10^{-6}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{13}B	$^{249}Cf(n, f)$	-	20.1 ± 1.1	$2.4\pm0.6\times10^{-6}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{14}B	$^{249}Cf(n, f)$	-	17.0 ± 1.2	$1.4\pm0.4\times10^{-6}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	¹⁵ B	$^{249}Cf(n, f)$	-	16.8 ± 1.9	$9.1 \pm 4.1 \times 10^{-6}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{14}C	$^{249}Cf(n, f)$	-	27.6 ± 0.3	$1.3\pm0.2\times10^{-5}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{15}C	$^{249}Cf(n, f)$	-	25.1 ± 0.5	$5.3\pm1.1\times10^{-6}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{16}C	$^{249}Cf(n, f)$	-	24.4 ± 1.1	$4.8\pm1.1\times10^{-6}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{17}C	$^{249}Cf(n, f)$	-	21.3 ± 1.7	$7.5\pm2.8\times10^{-7}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{18}C	$^{249}Cf(n, f)$	-	20.4 ± 2.8	$2.4\pm0.7\times10^{-7}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{16}N	$^{249}Cf(n, f)$	-	25.9 ± 2.2	$1.5\pm0.4\times10^{-7}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{17}N	$^{249}Cf(n, f)$	-	25.0 ± 1.6	$8.1\pm2.0\times10^{-7}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{18}N	$^{249}Cf(n, f)$	-	23.8 ± 1.5	$4.5\pm1.1\times10^{-7}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	20O	$^{249}Cf(n, f)$	-	31.4 ± 1.7	$25.0\pm0.7\times10^{-6}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	²¹ O	$^{249}Cf(n, f)$	-	24.2 ± 1.2	$6.4 \pm 1.3 \times 10^{-7}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	²² O	$^{249}Cf(n, f)$	-	33.0 ± 7.4	$4.2\pm1.6\times10^{-7}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{21}F	$^{249}Cf(n, f)$	-	26.0 ± 2.1	$1.6\pm0.4\times10^{-7}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{22}F	$^{249}Cf(n, f)$	-	33.8 ± 10.5	$1.4\pm0.8\times10^{-7}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	^{24}F	$^{249}Cf(n,f)$	-	26.3 ± 2.8	$8.3 \pm 4.0 \times 10^{-8}$
^{27}Na $^{249}Cf(n, f)$ - 38.4 ± 8.2 $8.2\pm3.2\times10^{-8}$ ^{30}Na $^{249}Cf(n, f)$ - 31.7 ± 8.6 $2.2\pm2.2\times10^{-8}$ ^{30}Mg $^{249}Cf(n, f)$ - 34.9 ± 3.7 $1.3\pm0.4\times10^{-7}$	^{24}Ne	$^{249}Cf(n,f)$	-	33.9 ± 2.9	$2.4\pm0.6\times10^{-7}$
${}^{30}Na$ ${}^{249}Cf(n, f)$ - ${}^{31.7\pm8.6}$ ${}^{2.2\pm2.2\times10^{-8}}$ ${}^{30}Mg$ ${}^{249}Cf(n, f)$ - ${}^{34.9\pm3.7}$ ${}^{1.3\pm0.4\times10^{-7}}$	^{27}Na	$^{249}Cf(n, f)$	-	38.4 ± 8.2	$8.2\pm3.2\times10^{-8}$
^{30}Mg $^{249}Cf(n, f)$ - $^{34.9\pm3.7}$ $^{1.3\pm0.4\times10^{-7}}$	^{30}Na	$^{249}Cf(n, f)$	-	31.7 ± 8.6	$2.2\pm2.2\times10^{-8}$
	^{30}Mg	$^{249}Cf(n,f)$	-	34.9 ± 3.7	$1.3\pm0.4\times10^{-7}$





Three cluster model is worked out in terms of:

- I. Mass asymmetry (η)
- II. Charge asymmetry (η_Z)
- III. Relative separation (**R**)
- IV. Deformation (β_2)
- V. Orientation angle (θ)

VI. Fragment mass number (A_3)





b) With β_2 , 90° - 90°





 $Q = E_1 + E_2 + E_3$ with Q-value for the three decay products defined as

$$Q = M - \sum_{i=1}^{N} m_i$$

M – Mass excess of decaying nucleus m – mass excesses of product nuclei.

The three body ternary fragmentation potential is defined as

$$V_{tot} = \sum_{i=1}^{3} \sum_{j>i}^{3} \left(B_{ii} + V_{ij} \right)$$

B_{ii} are binding energies

$$V_{ij} = V_{Cij} + V_{Nij}$$





The Coulomb interaction between the three spherical nuclei is given as

 $V_{Cij} = \frac{Z_i Z_j e^2}{R^s ::}$

For deformed and oriented case



 $\times \left| \beta_{\lambda k} + \frac{4}{7} \beta_{\lambda k}^2 Y_{\lambda}^{(0)}(\theta_k) \right|$



b) With β_2 , 90°-90°









With,

$$R^{s}_{ij} = R_{ij} + S_{ij}$$
$$R_{ij} = r_0 \left(A_i^{1/3} + A_j^{1/3} \right)$$

the relative separation between fragments,

Radius of the fragments

$$R_{0i} = 1.28A_i^{1/3} - 0.76 + 0.8A_i^{-1/3}$$
Spherical case
$$R_i(\alpha_i) = R_{0i} \left[1 + \sum_{\lambda} \beta_{\lambda i} Y_{\lambda}^{(0)}(\alpha_i) \right]$$
Deformed case



S_{ij} - surface separation

For touching configuration, $s=s_{12}=s_{13}=s_{23}=0$



Collinear configuration



$$s_{12} = s_{23} = s_{13} = s$$
 $s_{12} = s_{23} = s;$ $s_{13} = 2(R_2 + s)$



For attractive part

Nuclear interaction potential (V_{Nij})

Yukawa plus exponential potential (For spherical fragments)

$$V_{Nij} = -4\left(\frac{a}{r_0}\right)^2 \sqrt{a_{2i}a_{2j}} \times \left[g_i g_j \left(4 + \frac{R_{ij}}{a}\right) - g_j f_i - g_i f_j\right] \frac{\exp\left(-\frac{R_{ij}}{a}\right)}{\frac{R_{ij}}{a}}$$

Nuclear Proximity potential

(For deformed fragments)

$$V_P = 4\pi \overline{R} \gamma b \phi(\xi)$$



In TCM the decay constant and half-life are defined as

$$\lambda = PP_0P_3\upsilon; \qquad T_{\frac{1}{2}} = \frac{\ln 2}{\lambda}$$

 $v \rightarrow$ is the assault frequency

- $P_3 \rightarrow$ is the preformation probability of the third fragment (assumed to be equal to unity)
- $P_0 \rightarrow$ is the preformation probability of the other two fragments calculated by solving Schrodinger equation
- P→ is the penetration probability of the fragments to cross the interaction barrier $P = \frac{2^{s_2}}{12 \sqrt{y}} \left[2 \sqrt{y} \sqrt{y} \right]$

$$P = \exp \left| -\frac{2}{\hbar} \int_{s_1}^{s_2} \left\{ 2\mu [V(s) - Q] \right\}^{\frac{1}{2}} ds \right|$$

The relative yield for all the charge minimized ternary fragmentation channels are calculated $Y(A_i, Z_i) = \frac{P(A_i, Z_i)}{m}$

$$Y(A_i, Z_i) = \frac{P(A_i, Z_i)}{\sum P(A_i, Z_i)}$$





Californium (Cf) nuclei offer interesting possibilities for both the theoretical and experimental investigations of various spontaneous decay modes such as Spontaneous binary fission, ternary fission and cluster radioactivity.

Spontaneous ternary fissions of ²⁵²Cf have been recently studied quite extensively with ⁴He, ¹⁰Be and ¹⁴C nuclei as third particle.

The cold a-accompanied TF of ²⁵²Cf was recently observed by Ramayya et al in which the yields for correlated pair of Kr-Nd, Sr-Ce, Zr-Ba, Mo-Xe, Ru-Te, Pd-Sn associated with ⁴He as the third particle has been measured.

This experiment was the first evidence for the cold (neutron less) ternary fission.









2004 - 200

















In TCM, we are considering the heavy (A_1) and light (A_2) fragments as deformed (and the LCP (A_3) as spherical). Their interaction potentials are calculated by including these effects.

With incorporation of deformation,

we studied 90-90 (Belly-Belly) and 0-0 (Pole-Pole) orientations.







For Spherical case the deep minima in PES - Sn+ Pd+ He (⁴He accompanied TF of ²⁵²Cf)

The experimentally measured yields, has largest yields for the fragment combinations like Zr-Ba, Sr-Ce.

With deformation and orientation included the minima in spherical case were no longer present rather new cold valleys are seen in the PES.



















These results clearly shows that, the inclusion of deformation indeed increases the yield values favourable to the experimental values and in particular corresponding to 90-90 orientation matches well with that of experimental results.



- ◆If a system A undergoes ternary fission it can have thousands possibilities with respect mass asymmetries and charge asymmetries.
- To avoid the repetition of fragmentation $A_1 \ge A_2 \ge A_3$
- ◆All the possible ternary fragmentations of ²⁵²Cf in two different configurations (Equatorial and Collinear) are studied

***** The third fragment can have mass number $A_3 = 1$ to 84.











Equatorial configuration		Collinear configuration			Equatorial configuration			Collinear configuration			
Fragmentation channel	$V(\eta)$	Q value	Fragmentation channel	$V(\eta)$	Q value	Fragmentation channel	$V(\eta)$	Q value	Fragmentation channel	$V(\eta)$	Q value
	(MeV)	(MeV)		(MeV)	(MeV)		(MeV)	(MeV)		(MeV)	(MeV)
¹³⁰ Sn+ ¹²¹ Cd+ ¹ n	97.51	229.36	¹³⁰ Sn+ ¹²¹ Cd+ ¹ n	102.23	229.36	¹³⁴ Te+ ⁸² Ge+ ³⁶ Si	152.86	237.22	¹³⁴ Te+ ⁸² Ge+ ³⁶ Si	124.88	237.22
¹³¹ Sn+ ¹¹⁹ Ag+ ² H	117.59	218.76	¹⁸¹ Sn+ ¹¹⁹ Ag+ ² H	118.49	218.76	¹³³ Sb+ ⁸² Ge+ ³⁷ P	155.90	239.48	¹³³ Sb+ ⁸² Ge+ ³⁷ P	123.83	239.48
¹³³ Sb+ ¹¹⁶ Pd+ ³ H	114.26	219.80	¹³³ Sb+ ¹¹⁶ Pd+ ³ H	116.20	219.80	$^{132}Sn + ^{82}Ge + ^{38}S$	155.76	244.79	$^{134}\text{Te} + ^{80}\text{Zn} + ^{38}\text{S}$	124.25	238.81
¹³² Sn+ ¹¹⁶ Pd+ ⁴ He	111.05	229.76	¹³² Sn+ ¹¹⁶ Pd+ ⁴ He	110.58	229.76	$^{131}Sn + ^{82}Ge + ^{39}S$	157.76	237.47	$^{134}\text{Te} + ^{79}\text{Zn} + ^{39}\text{S}$	125.44	236.77
¹⁸¹ Sn+ ¹¹⁶ Pd+ ⁵ He	116.82	221.95	¹³¹ Sn+ ¹¹⁶ Pd+ ⁵ He	117.47	221.95	¹³⁴ Te+ ⁷⁸ Zn+ ⁴⁰ S	154.47	240.69	$^{134}\text{Te} + ^{78}\text{Zn} + ^{40}\text{S}$	121.73	240.69
¹³⁰ Sn+ ¹¹⁶ Pd+ ⁶ He	119.85	218.73	¹³⁰ Sn+ ¹¹⁶ Pd+ ⁶ He	120.71	218.73	¹³⁴ Te+ ⁷⁷ Zn+ ⁴¹ S	157.69	237.37	¹³³ Sb+ ⁷⁸ Zn+ ⁴¹ Cl	124.62	240.85
¹³³ Sb+ ¹¹² Ru+ ⁷ Li	128.28	215.44	¹³³ Sb+ ¹¹² Ru+ ⁷ Li	126.65	215.44	$^{134}\text{Te} + ^{76}\text{Zn} + ^{42}\text{S}$	155.34	239.70	$^{132}Sn + ^{78}Zn + ^{42}Ar$	123.04	245.37
¹³² Sn+ ¹¹² Ru+ ⁸ Be	129.16	222.85	¹³² Sn+ ¹¹² Ru+ ⁸ Be	124.22	222.85	¹³³ Sb+ ⁷⁶ Zn+ ⁴³ Cl	157.73	242.16	¹³³ Sb+ ⁷⁶ Zn+ ⁴³ Cl	123.80	242.16
¹³¹ Sn+ ¹¹² Ru+ ⁹ Be	132.68	217.59	¹³¹ Sn+ ¹¹² Ru+ ⁹ Be	128.70	217.59	¹³² Sn+ ⁷⁶ Zn+ ⁴⁴ Ar	156.76	247.83	$^{134}\text{Te} + ^{74}\text{Ni} + ^{44}\text{Ar}$	120.61	241.11
¹³⁴ Te+ ¹⁰⁸ Mo+ ¹⁰ Be	129.67	218.00	¹³⁴ Te+ ¹⁰⁸ Mo+ ¹⁰ Be	125.88	218.00	¹³¹ Sn+ ⁷⁶ Zn+ ⁴⁵ Ar	157.91	246.44	¹³⁴ Te+ ⁷³ Ni+ ⁴⁵ Ar	121.83	240.14
¹³⁴ Te+ ¹⁰⁷ Mo+ ¹¹ Be	135.48	212.01	$^{133}Sb+^{108}Mo+^{11}B$	130.85	217.61	¹³⁴ Te+ ⁷² Ni+ ⁴⁶ Ar	154.55	244.24	¹³⁴ Te+ ⁷² Ni+ ⁴⁶ Ar	118.02	244.24
¹³⁴ Te+ ¹⁰⁶ Mo+ ¹² Be	137.01	210.77	$^{132}Sn + ^{108}Mo + ^{12}C$	123.54	223.72	¹³³ Sb+ ⁷² Ni+ ⁴⁷ K	157.22	241.56	¹³³ Sb+ ⁷² Ni+ ⁴⁷ K	119.18	245.88
¹³³ Sb+ ¹⁰⁶ Mo+ ¹³ B	139.07	214.96	$^{132}Sn + ^{107}Mo + ^{13}C$	130.54	222.17	¹³⁴ Te+ ⁷⁰ Ni+ ⁴⁸ Ar	155.81	243.02	¹³² Sn+ ⁷² Ni+ ⁴⁸ Ca	115.93	251.84
$^{132}Sn + ^{106}Mo + ^{14}C$	135.08	225.94	$^{134}\text{Te} + ^{104}\text{Zr} + ^{14}\text{C}$	126.28	223.20	¹³¹ Sn+ ⁷² Ni+ ⁴⁹ Ca	157.44	250.07	¹³¹ Sn+ ⁷² Ni+ ⁴⁹ Ca	117.60	250.07
$^{134}\text{Te} + ^{103}\text{Zr} + ^{15}\text{C}$	139.90	218.27	$^{134}\text{Te} + ^{103}\text{Zr} + ^{15}\text{C}$	131.15	216.90	¹³² Sn+ ⁷⁰ Ni+ ⁵⁰ Ca	155.07	252.48	¹³² Sn+ ⁷⁰ Ni+ ⁵⁰ Ca	115.90	252.48
$^{134}\text{Te} + ^{102}\text{Zr} + ^{16}\text{C}$	139.55	218.46	$^{134}\text{Te} + ^{102}\text{Zr} + ^{16}\text{C}$	131.07	218.46	¹³¹ Sn+ ⁷⁰ Ni+ ⁵¹ Ca	157.43	249.94	¹³¹ Sn+ ⁷⁰ Ni+ ⁵¹ Ca	118.38	249.94
$^{133}Sb+^{102}Zr+^{17}N$	144.78	219.96	$^{133}Sb+^{102}Zr+^{17}N$	133.66	219.96	¹³⁰ Sn+ ⁷⁰ Ni+ ⁵² Ca	157.68	249.56	¹³⁴ Te+ ⁶⁶ Fe+ ⁵² Ca	117.88	243.36
$^{132}Sn + ^{102}Zr + ^{18}O$	145.64	226.05	$^{132}Sn + ^{102}Zr + ^{18}O$	131.74	226.05	¹³³ Sb+ ⁶⁶ Fe+ ⁵³ Sc	160.96	244.49	¹³³ Sb+ ⁶⁶ Fe+ ⁵³ Sc	119.34	244.49
$^{182}Sn + ^{101}Zr + ^{19}O$	147.79	216.67	$^{131}Sn + ^{102}Zr + ^{19}O$	134.45	223.08	$^{132}Sn + ^{66}Fe + ^{54}Ti$	159.72	249.72	$^{132}Sn + ^{66}Fe + ^{54}Ti$	116.58	249.72
$^{132}Sn + ^{100}Zr + ^{20}O$	144.61	226.17	$^{134}\text{Te} + ^{98}\text{Sr} + ^{20}\text{O}$	130.83	223.24	$^{131}Sn + ^{66}Fe + ^{55}Ti$	162.32	246.91	$^{131}Sn + ^{66}Fe + ^{55}Ti$	119.31	246.91
$^{134}Sn + ^{100}Zr + ^{21}O$	147.18	220.58	¹³⁴ Te+ ⁹⁷ Sr+ ²¹ O	133.63	220.58	$^{130}Sn + {}^{66}Fe + {}^{56}Ti$	161.83	247.23	$^{134}\text{Te} + ^{62}\text{Cr} + ^{56}\text{Ti}$	118.87	239.64
¹³⁴ Te+ ⁹⁶ Sr+ ²² O	144.74	223.05	¹³⁴ Te+ ⁹⁶ Sr+ ²² O	131.39	223.05	$^{131}Sn + {}^{64}Fe + {}^{57}Ti$	165.13	244.14	$^{133}Sb + {}^{62}Cr + {}^{57}V$	120.38	240.55
¹³⁴ Te+ ⁹⁵ Sr+ ²³ O	149.10	218.90	$^{133}Sb + ^{96}Sr + ^{23}F$	133.52	224.68	¹³⁴ Te+ ⁶⁰ Cr+ ⁵⁸ Ti	163.76	238.81	¹³² Sn+ ⁶² Cr+ ⁵⁸ Cr	117.69	245.55
¹³² Sn+ ⁹⁶ Sr+ ²⁴ Ne	148.79	231.40	¹³² Sn+ ⁹⁶ Sr+ ²⁴ Ne	130.58	231.40	$^{133}Sb + {}^{60}Cr + {}^{59}V$	165.56	240.82	$^{131}Sn + ^{62}Cr + ^{59}Cr$	120.53	242.62
¹³¹ Sn+ ⁹⁶ Sr+ ²⁵ Ne	151.25	228.66	¹³⁴ Te+ ⁹³ Kr+ ²⁶ Ne	132.98	224.72	$^{132}Sn + ^{60}Cr + ^{60}Cr$	162.83	247.17	$^{132}Sn + ^{60}Cr + ^{60}Cr$	116.87	247.17
¹³⁴ Te+ ⁹² Kr+ ²⁶ Ne	149.55	226.85	¹³⁴ Te+ ⁹² Kr+ ²⁶ Ne	131.02	226.85	$^{130}Sn + ^{61}Cr + ^{61}Cr$	165.63	242.04	$^{130}Sn + ^{61}V + ^{61}Mn$	121.32	239.49
¹³³ Sb+ ⁹² Kr+ ²⁷ Na	153.92	228.53	¹³³ Sb+ ⁹² Kr+ ²⁷ Na	133.00	228.53	$^{128}Sn + ^{62}Cr + ^{62}Cr$	167.35	242.09	$^{128}Sn + ^{62}Cr + ^{62}Cr$	120.91	242.09
¹³² Sn+ ⁹² Kr+ ²⁸ Mg	153.04	235.41	¹³² Sn+ ⁹² Kr+ ²⁸ Mg	129.73	235.41	¹²⁶ Cd+ ⁶³ Mn+ ⁶³ Mn	173.23	242.75	¹²⁵ Cd+ ⁶⁴ Cr+ ⁶³ Fe	125.64	240.60
¹³² Sn+ ⁹¹ Kr+ ²⁹ Mg	155.40	232.71	¹³⁵ Te+ ⁸⁸ Se+ ²⁹ Mg	131.90	228.49	¹¹⁰ Mo+78Zn+64Fe	172.74	243.00	¹²⁴ Cd+ ⁶⁴ Cr+ ⁶⁴ Fe	123.16	243.00
¹³⁴ Te+ ⁸⁸ Se+ ³⁰ Mg	152.60	231.38	¹³⁴ Te+ ⁸⁸ Se+ ³⁰ Mg	128.92	231.38	¹⁰⁹ Mo+ ⁷⁸ Zn+ ⁶⁵ Fe	176.15	245.44	¹²¹ Pd+ ⁶⁶ Fe+ ⁶⁵ Fe	128.60	245.44
¹³⁶ Te+ ⁸⁶ Se+ ³¹ Mg	155.90	228.05	¹³³ Sb+ ⁸⁸ Se+ ³¹ Mg	130.68	226.27	¹⁰⁴ Zr+ ⁸² Ge+ ⁶⁶ Fe	173.07	258.73	¹²⁰ Pd+ ⁶⁶ Fe+ ⁶⁶ Fe	125.81	248.18
¹³⁴ Te+ ⁸⁶ Se+ ³² Mg	153.54	230.30	¹³² Sn+ ⁸⁸ Se+ ³² Si	127.54	239.69	1037r + 82Ce + 67Fe	174.81	256.91	¹¹⁷ Pd+ ⁶⁸ Fe+ ⁶⁷ Fe	128.83	244.31
¹³² Sn+ ⁸⁷ Se+ ³³ Si	155.70	233.68	¹³⁵ Te+ ⁸⁴ Ge+ ³³ Si	128.61	233.21	102Zr $+$ ⁸² Ce $+$ ⁶⁸ Fe	173 11	258.59	104Zr $+$ ⁸⁰ Zn $+$ ⁶⁸ Ni	126.76	259.02
¹³² Sn+ ⁸⁶ Se+ ³⁴ Si	152.26	242.57	¹³⁴ Te+ ⁸⁴ Ge+ ³⁴ Si	124.35	237.34	$^{102}Z_{r} + {}^{81}G_{s} + {}^{69}C_{o}$	174.62	257.80	$109M_{0}+74N_{1}+69N_{1}$	127.87	253.20
¹³⁴ Te+ ⁸³ Ge+ ³⁵ Si	155.72	234.47	¹³³ Sb+ ⁸⁴ Ge+ ³⁶ P	127.10	237.92	¹⁰² Zr+ ⁸⁰ Zn+ ⁷⁰ Ni	172.00	260.96	¹⁰² Zr+ ⁸⁰ Zn+ ⁷⁰ Ni	124.72	260.96







The relative yield corresponding to equatorial emission lies above the relative yield corresponding to the collinear emission of fragments up to third fragments with mass number A_3 = 38 and beyond that the yield corresponding to collinear emission lies well above the relative yield of equatorial emission.

Light fragments prefer the equatorial emission and the heavy fragments prefer the collinear emission.

In particular the relative yield corresponding to the fragment ⁴⁸Ca and its neighboring nuclei is larger in collinear emission.











